

Introduction into cost-benefit analysis

CONTENT

INTRODUCTION

- The concept of “investment”
- Management steps

BASICS OF DISCOUNTING

FINANCIAL EVALUATION METHODS

- Net present value method (NPV)
- Internal rate of return (IRR)
- Payback method

- Case -

Introduction into cost-benefit analysis

CONTENT

VALUE ANALYSIS

- Definition of objectives
 - Weighting of objectives
 - Quantification of values
- Case

CALCULATION OF ECONOMICS RATE OF RETURN

- Relevant costs
 - Valuation of costs and benefits
- Case

Introduction into cost-benefit analysis

CONTENT

SENSITIVITY ANALYSIS

RELEVANCE OF CBA FOR AN AUDITOR

- Legal background
- List of typical type of projects
- What items can be verified ?
- Possible conclusions for the auditor

Introduction into cost-benefit analysis

INVESTMENT

DEFINITION

↓ Investment:

the act of placing funds in other form capital

or

to place funds in non-financial assets in order
to achieve financial or non-financial return

Introduction into cost-benefit analysis

INVESTMENT

- limited period of using investment
 - **technical life-time (economic life-time)**
- induced financial flows
 - **costs**
 - **revenues**
- uncertainty

Introduction into cost-benefit analysis

INVESTMENT

DECISION PROBLEM

1. Is an investment profitable ?
2. What is the most profitable alternative ?

MANAGEMENT STEPS

Step 1: Identification and description of the project

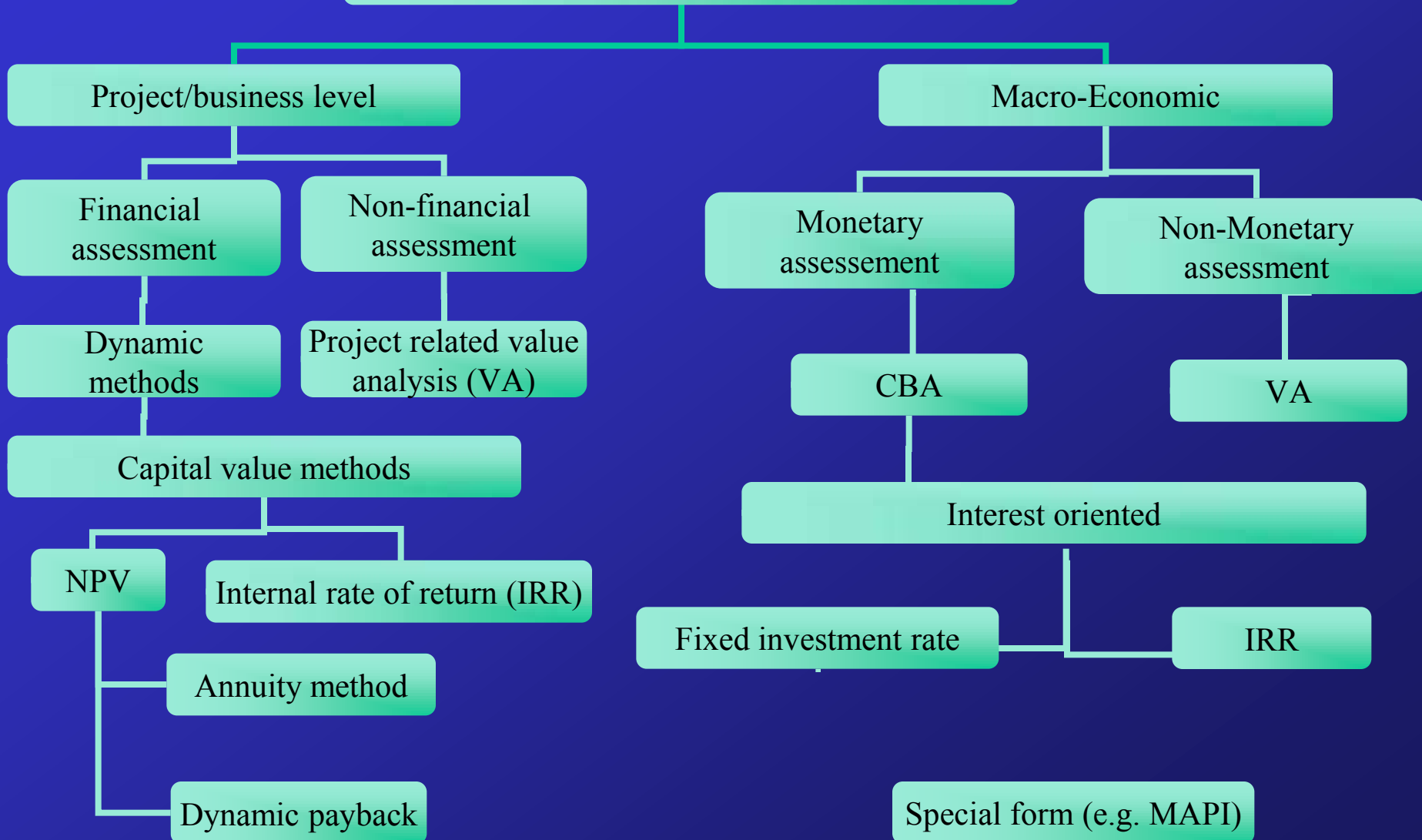
Step 2: Ex-ante evaluation

Step 3: Decision making process

Step 4: Realisation of the investment

Step 5: Ex-post evaluation

Investment analysis



Basic of discounting

Principle : 1 EURO spent in the future has less value today

OR 1 EURO spent today has higher value in the future

Definitions :

C_0 = capital (present) value at the beginning of an investment period

C_n = capital value at the end of an investment period

t = 1, 2, ..., n year (n = last year)

i = discount rate

a_0 = initial investment

R_n = residual value of an investment after n-years

A = annuity

Calculation examples

- I. Investment amount 1.000
- Interest rate 0,05 (=5%)
- duration 3 years

1. Year end: $1.000 + 1.000 * 0,05 = 1.050$ or
 $1.000 * (1 + 0,05) = 1.050$

2. Year end: $1.050 + 1.050 * 0,05 = 1.102,5$ or
 $1.000 * (1 + 0,05) * (1 + 0,05) =$
 $1.000 * (1 * 0,05)^2 = 1.102,5$

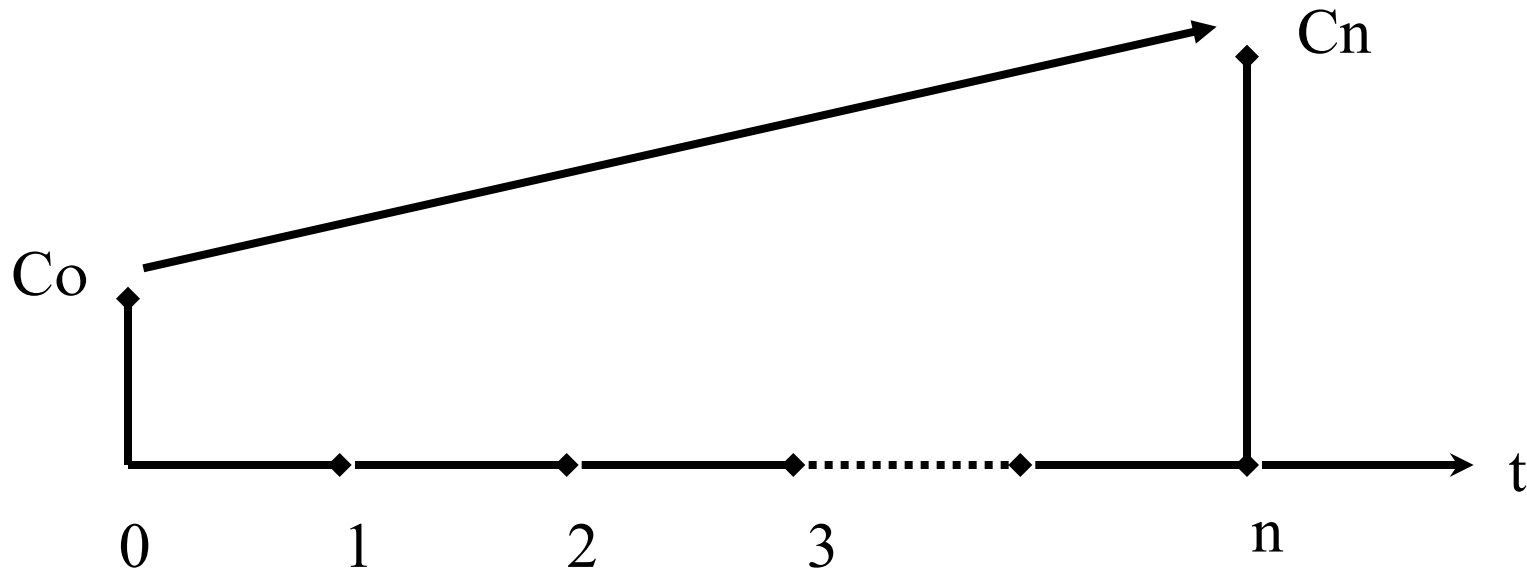
3. Year end $1.102,5 + 1.102,5 * 0,05 = 1.157,63$ or
 $1.000 * (1 + 0,05) * (1 + 0,05) * (1 + 0,05)$
 $1.000 * (1 + 0,05)^3 = 1.157,63$

*Or $1.000 * 1/\text{discount factor } (t=3 I=5) = 1.000 * 1/0,864 = 1.157,4$*

Interpretation of result

- The start capital of 1.000 is after 3 years 1.157,63 worth; the present value is increased in the future
- *Or* an value of 1.157,63 end of three years from the present would have a worth at present of 1.000; the future value is less worth at present

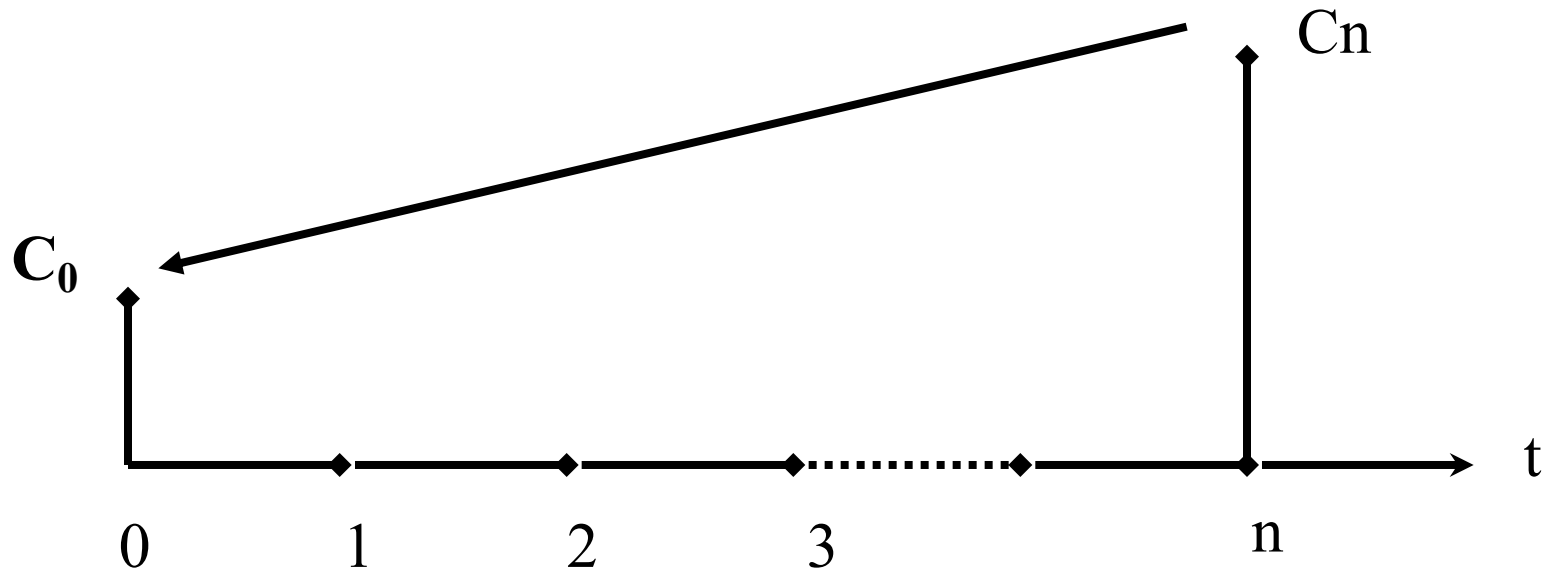
1. Calculation of the end-value C_n



Factor : $r^n = (1 + i)^n$

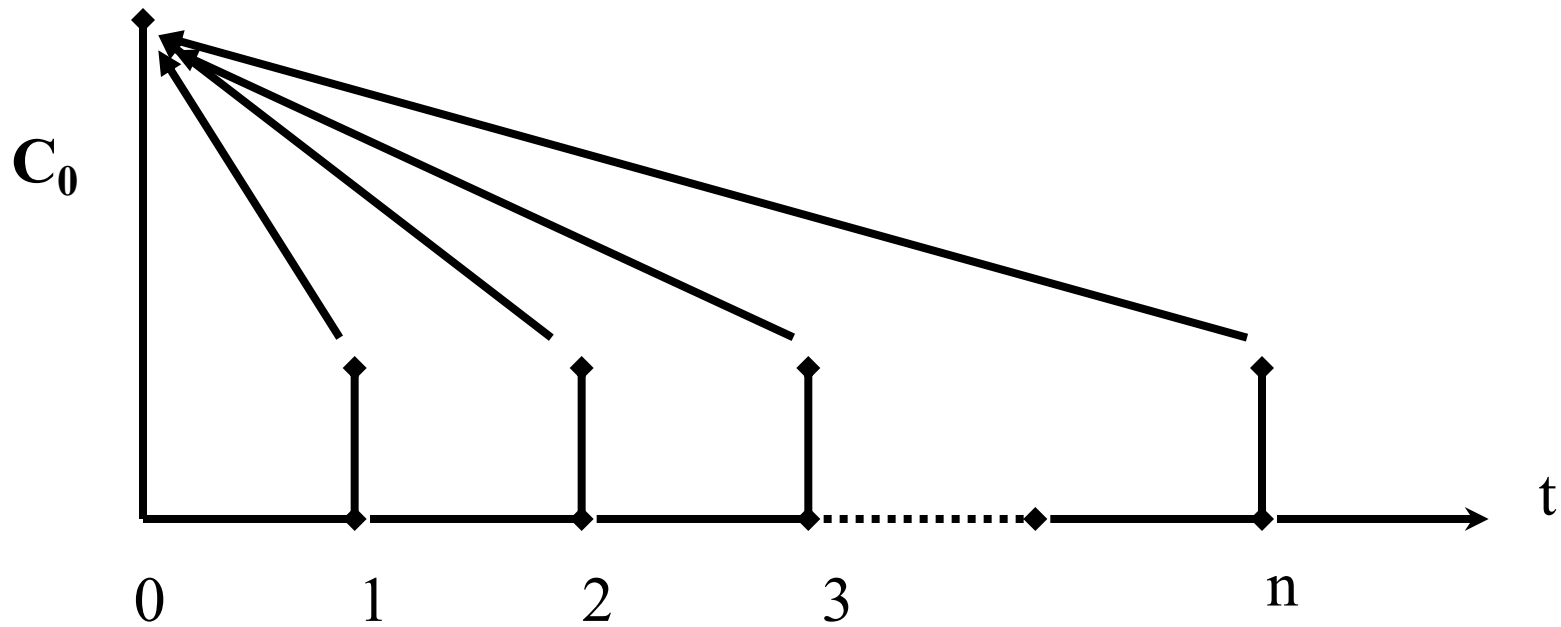
$C_n = C_0 \times r^n$

2. Net value C_0 calculated by discounting



Factor : $y^n = 1/r_n$ $C_0 = C_n \times y^n$

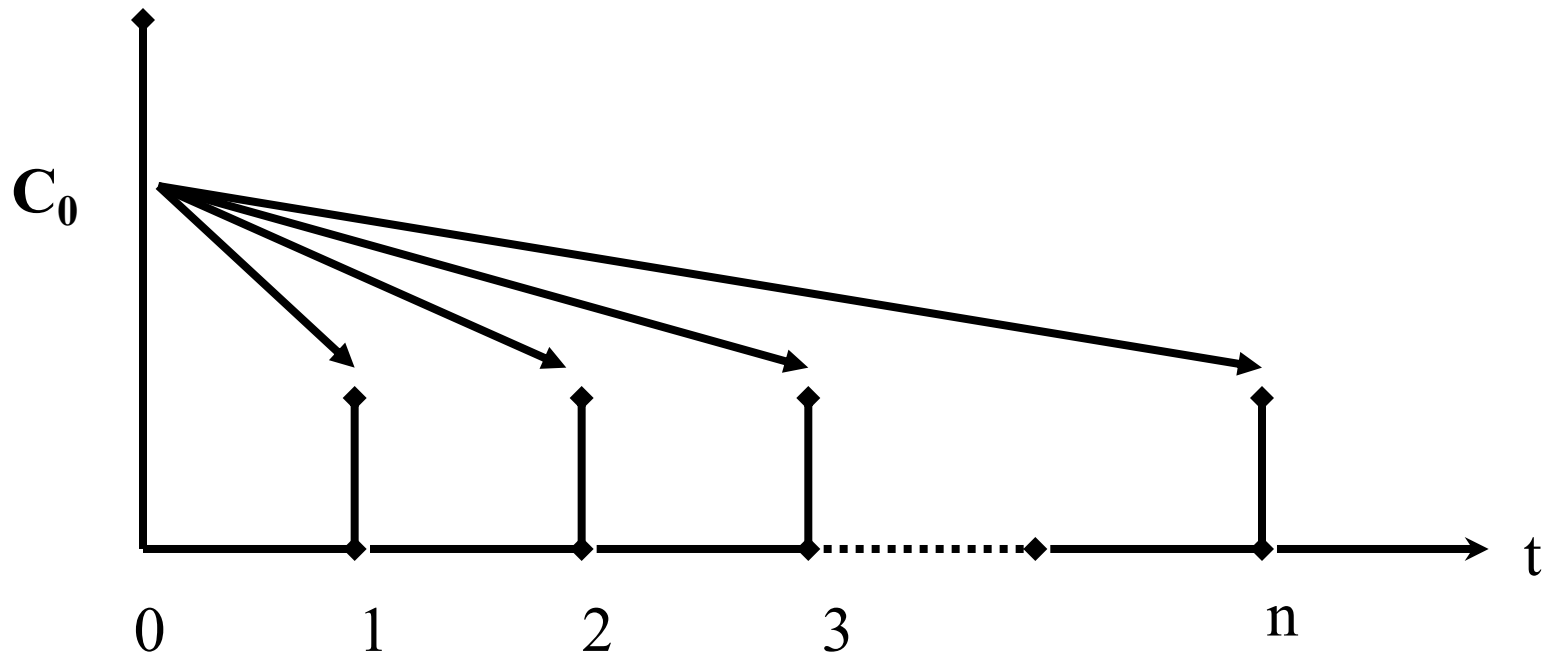
3. Net value of an annuity



Factor : $\frac{(1 + i)^n - 1}{(1 + i)^n \times i} = a_n$

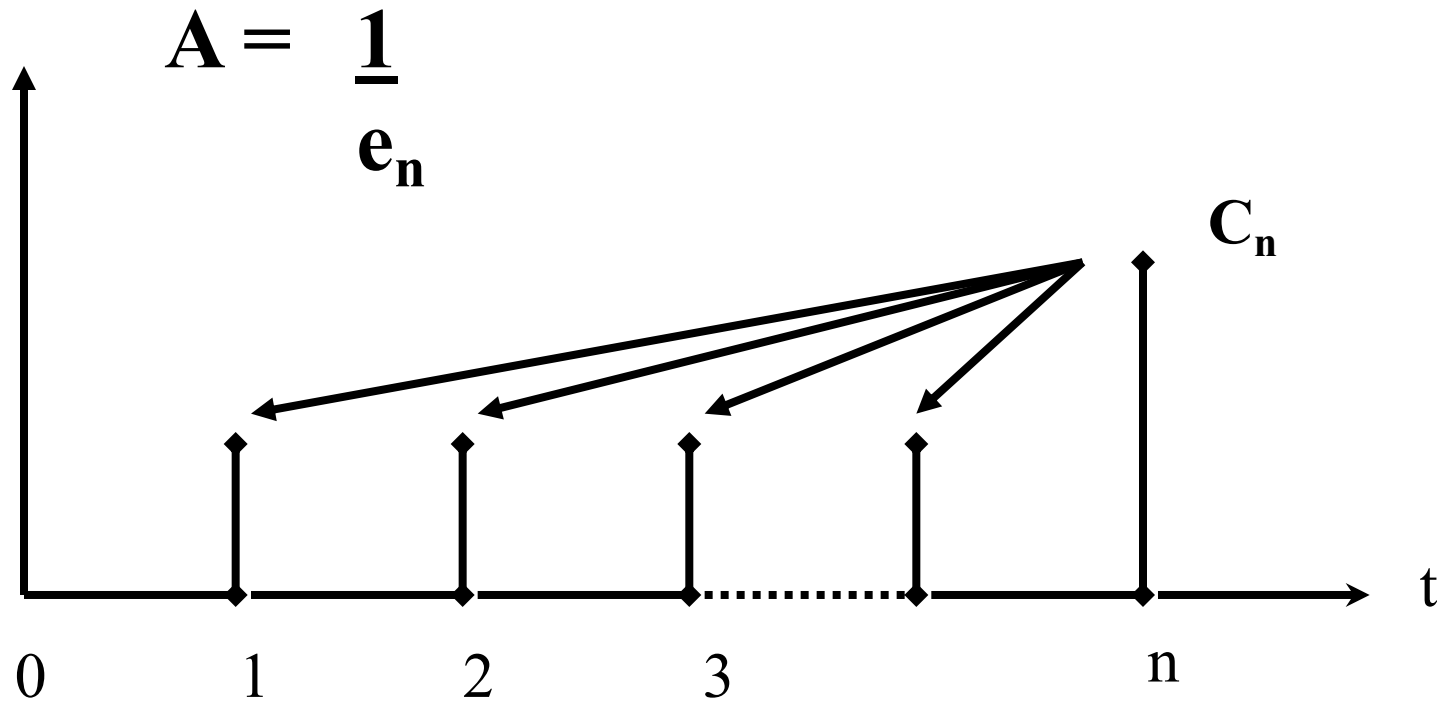
$C_0 = A_c \times a_n$

4. Annuity for interest of i and payback C_0



Recovery factor : $y^n = \frac{1}{a_n}$ $A = C_0 \times \frac{1}{a_n} = C_0 \times \text{RF}$

6. Annuity A of a final value C_n



Factor : $\frac{i}{(1+i)^n - 1} = \frac{i}{(r_n - 1)} = \frac{1}{e_n}$

How to proceed with the NPV methode

- determine the available amount and the calculation rate (alternative rate for placing funds in the capital market)
- determine duration of the investment
- determine the expected cash flows (costs; revenues) and the residual value at the end of the periode
- Discount the flows to receive the NPV

Decision criteria for NPV

- **An investment is profitable if the $NPV \geq 0$**
- **With alternatives the investment with the biggest $NPV \geq 0$ is preferred**

How to proceed for calculating the IRR

- determine available capital, expected duration, estimate the cash flows over the time, estimate the residual value
- One wants to get the rentabilitiy of the investement
- The internal rate is the rate, for which the NPV becomes 0 .
- Solutions: a) interpolation
 - b) graphical
 - c) approximation

Decision criteria for IRR

- Profitable if the IRR of bigger than the calculation rate
- for alternatives : the biggest IRR is the most profitable project

Pay-Back period

- A project is profitable if the cumulated cash flow over the life-time exceeds the initial investment
- If various investment alternatives : the project with the shortest pay-back period will be referred

Case 1

- 4 alternative investments with following data:
each has amount of 20.000 to invest
constant annual **revenue (costs)** for
alternative one 18.000.-(6.000), two 20.000.-
(10.000), three 12.000.-(4.000), and four
10.000.-(4.000)

The alternatives have following life time in years: 3,
5, 7, 9

- The calculation rate is 0,08 (8%)
- Find the NPVs, IIRs and payback periodes.

Basics about Value Analysis

- **objective hierarchy**
- **utility function**
- **weighting of objectives**
- **transformation function**
- **nominale – ordinale – cardinale**

Basics about Value Analysis

- **Procedural steps:**
 - **definition of target criteria**
 - **weighting of target criteria**
 - **identification of subvalue/utility**
 - **Total value**
 - **Assessment of advantage**

Basics about Value Analysis

- **Road alternative 1 A1**
- **Road alternative 2 A 2**
 - **Time saving T weight g1 0,3**
 - **security S weight g2 0,4**
 - **location advantage L weight g3 0,3**

Assumptions in Value Analysis

- **Value independent target criteria**
- **value/utility is measurable (cardinal)**
- **only feasible alternatives are analysed (financial and economic upper and lower bounds are given)**

Links of capital value and benefit value

1. $C_0 \geq 0$ and $N \geq \underline{N}$

2. $C_0 \leq 0$ and $N < \underline{N}$

3. $C_0 < 0$ and $N > \underline{N}$

4. $C_0 > 0$ and $N < \underline{N}$

With C_0 : financial value of an investment

N : benefit (non-financial) value of an investment

\underline{N} : subjective minimum of value to be achieved

Preparatory steps for the financial analysis

- ✓ Determine the project alternatives
- ✓ Assess the price for the initial investment
- ✓ Estimation of life-time
- ✓ Estimation of the periodical costs
- ✓ Estimation of the periodical revenues
- ✓ Estimation of the residual value
- ✓ Determination of the calculation rate

Decision criteria for IRR

- Profitable if the IRR of bigger than the calculation rate
- for alternatives : the biggest IRR is the most profitable project

Steps to calculate the IRR

1. Classical approach

- compute NPV_1 with one calculation rate r_1
- if the NPV_1 is negative (positive) take another rate r_2 , r_3 , ... until the NPV_2 becomes positive (negative)
- make a graphical interpolation to find the intersection of the IRR which makes the $NPV = 0$ the rate which leads to $NPV = 0$ is the IRR

2. Simplified approach

$$IRR = r_1 - NPV_1 (r_2 - r_1) / (NPV_2 - NPV_1)$$

Some assumptions

- ❖ Returned capital will be placed on the capital market on the calculation rate
- ❖ Unlimited credit for the calculation rate would be available all over the time

Some Aspects of E-CBA

- **shadow prices**
- **opportunity costs**
- **what are labour costs?**
- **where to get data?**

Checklist for audit - 1

- **What type and at what stage do rules foresee CBA?**
- **Who did CBA?**
- **When was it done?**
- **Which methode?**
- **Which calculation rate and how justified?**

Checklist for audit -2

- **Justification for time horizon?**
- **Which costs taken into account?**
- **How was estimated revenue achieved?**
- **CBA well documented?**
- **All assumptions listed?**
- **CBA for economic and financial calculation?**

Checklist for audit -3

- **For economic CBA: are shadow prices and costs listed and which source were taken?**
- **Was a sensitivity analysis made? Which results?**
- **Were alternatives considered?**
- **Final decision corresponds to CBA result? If not why not?**